Coordinated Broadcasting for Multiuser Indoor Visible Light Communication Systems

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Abstract—Visible light communication (VLC) re-uses illumination devices, in particular light-emitting diodes (LEDs), for communication purposes. It has great potential to alleviate the strain on radio frequency spectrum in indoor environments. VLC-enabled LED luminaries form VLC attocells that carry downlink traffic to indoor mobile or stationary terminals. While one of the advantages of indoor VLC is low interference due to natural cell boundaries such as walls, multiple VLC attocells within a room would interfere. This is because illumination requirements often mandate a rich overlap of emissions of luminaries in a room. In this paper, we suggest the coordination of multiple VLC attocells (i.e., VLC-enabled LED luminaries) to turn the problem of overlap and thus interference into an advantage. We stipulate that this coordination can be accomplished through power line communication (PLC), which has been considered before as a means to transport data to VLC transmitters. Borrowing from concepts developed for radio-frequency wireless communications, we develop several precoding schemes for the new coordinated VLC broadcasting architecture. These include designs for the case of imperfect channel knowledge at the VLC transmitter, since channel information is usually provided through a low-rate feedback channel. The performance advantages for VLC transmission due to the proposed coordination and precoding designs are demonstrated based on a set of numerical results.

Index Terms—Visible light communication (VLC), multiuser communications, precoding, broadcasting, imperfect channel state information.

I. INTRODUCTION

Wireless data traffic is increasing at a fast pace, with most of the traffic being generated in homes, office buildings and other indoor spaces [2]. The creation of small-cell networks and operation of heterogeneous networks are two means to address this problem. However, eventually the usable radio-frequency (RF) spectrum is a finite resource and inter- and intra-cell interference are limiting wireless network capacity.

A mostly untapped resource that could alleviate the strain on RF spectrum is optical wireless communication (OWC), and in particular visible light communication (VLC) for indoor wireless transmission. VLC operates over the license-free visible spectrum and thus does not cause interference to RF wireless signals. Also interference between VLC transmitters is confined to within rooms or otherwise walled areas. VLC uses light-emitting diodes (LEDs) as the transmitting devices. The information-carrying signal modulates the light carrier by varying illumination intensity, i.e., the brightness of the LED signal, fast enough to be imperceptible by humans. Since LEDs are replacing incandescent bulbs and fluorescent lamps for illumination, VLC emitters will be ubiquitously available.

At the receiver side, an inexpensive photodetector converts the optical signals into electrical signals to decode the information. Thus, virtually any device can be enabled to become a VLC receiver at minimal cost. Furthermore, both industrial activity and standardization around VLC is rapidly maturing, cf. e.g. [3], [4].

The integration of VLC into an indoor communication network establishes optical attocells [5], responsible for the downlink traffic from network to user terminals. These attocells could be easily deployed wherever LEDs are adopted for illumination, including in electromagnetic interference sensitive areas like hospitals and airplanes. Although opaque boundaries effectively contain light signals, VLC attocells would generally not operate free of interference. Illumination designers aim to have a uniform illumination at a certain height in a room. This mandates a rich overlap between the emissions of luminaries to make illumination more uniform. Therefore, interference between VLC emitters is unavoidable.

Fortunately, this interference will be spatially limited to neighboring or nearby attocells.

In this paper, we consider VLC attocell systems and propose the coordination of different transmitters, i.e., LED luminaries, through a backbone network. The purpose of this coordination is to turn unwanted interference into constructive signal components. The backbone could be realized by a wired Ethernet or power-over-Ethernet link. Another convenient manner to realize the backbone is using existing electrical power wiring for data communications, i.e., power line communications (PLC) [6]. The concept of integrating PLC and VLC to form a hybrid system for fast data delivery to users in indoor office buildings and homes is not new [7]–[9]. However, we suggest that since multiple LED luminaries in the same room are connected to the same power wires, PLC can be used to serve as a backbone network to support the cooperation among multiple VLC attocells. This was first mentioned in our conference paper [10], and can be considered as the VLC counterpart to coordinated multipoint (CoMP) in RF cellular networks [11].

Multiple coordinated VLC emitters form a virtual multiple-transmitter (or multiple-“antenna”) system. In this paper, we focus on the signal processing required at the VLC transmitters...
to benefit from coordination [1]. We note that this is quite different from the indoor multiple-input multiple-output (MIMO) VLC systems for point-to-point communication studied in [12], [13], as we are dealing with broadcasting of data to multiple VLC receivers (e.g., cellular phones or tablets) employing single photodiode receivers. Such multiuser multiple-input single-output (MU-MISO) systems have widely been studied for radio communication systems, cf., e.g., [14]–[16]. However, different from RF wireless communication, VLC uses intensity modulation and the transmitted signal must be non-negative and constrained in mean amplitude, i.e., average optical power. These differences render solutions developed for the RF case not directly applicable to VLC systems. We investigate the effect of different levels of coordination of luminaries in a room, leading to different numbers of attocells and intercell-interference scenarios. Within a coordinated broadcasting system, linear minimum mean-squared error (MMSE) precoder design is applied. This allows us to consider interference from adjacent VLC transmitters that are not coordinated, as well as ambient light from the sun and other non-VLC lighting devices. Furthermore, we extend our design to the case of imperfect knowledge of the VLC transmission channel. Our numerical results highlight the benefits of coordination for VLC attocell systems by demonstrating significant gains in achievable signal-to-interference-plus-noise ratio (SINR).

The remainder of the paper is organized as follows. In Section II, we propose a coordinated VLC system architecture with PLC as its backbone network. In Section III, precoder design strategies for VLC MU-MISO transmission with perfect channel state information (CSI) at the transmitter are developed. In Section IV, the designs are extended to the case of imperfect CSI. Simulation results are presented and discussed in Section V, and finally we conclude this paper in Section VI.

The following notations are used in this paper. Bold uppercase and lower case letters are used to denote matrices and vectors, respectively. vec(·) is the vectorization operator, ⊗ represents the Kronecker product, and and 1 are the identity matrix and all-one vector of appropriate size, respectively. \( \| \cdot \|_p \) represents the p-norm, \( [ \cdot ]^T \) is the transpose operator, and \( E(\cdot) \) denotes statistical expectation.

II. COORDINATED VLC BROADCASTING

We consider an indoor environment with multiple LED luminaries deployed in a room, office, laboratory or similar indoor space. The main elements of the coordinated VLC broadcast system are illustrated in Figure 1. The luminaries function as VLC transmitters as a secondary use, and they receive electricity and data through a PLC backbone network. This enables some of the VLC transmitters, e.g., those connected to the same distribution box, to operate in a coordinated fashion alike CoMP. Similar to the definition of a CoMP-cell in the context of RF wireless systems [11], we define a

CoMP-attocell as the area covered by one VLC broadcasting system where all the transmitters are coordinated by the PLC backbone network. In the case of multiple CoMP-attocells in one room, there is interference from neighbouring CoMP-attocells, which is analogous to inter-CoMP-cell interference in RF cellular systems.

A. VLC Channel

Before discussing the broadcast transmission and VLC-specific constraints, we first briefly elaborate on channel gain and noise models applicable to intensity modulation (IM) at the transmitter and direct detection (DD) at the receiver (IM/DD).

Each LED luminary has \( K \) LED elements with a Lambertian radiation pattern. We consider the use of commercial off-the-shelf LEDs, whose bandwidth can reach up to 20 MHz [18]. In this case, multipath delay resulting from wall reflections and the path difference among spatially separated LED luminaries can be ignored and the VLC channel can be approximated as a single-tap channel. The channel gain \( h_{kn} \) between the \( k_{th} \) receiver and the \( n_{th} \) LED luminary can be expressed as [19]

\[
h_{kn} = \sum_{i=1}^{K} G_{ki} A_k R(\phi_{kn}) T(\psi_{kn}) \cos(\psi_{kn}) \mathbb{I}_A(\psi_{kn}),
\]

where \( G_{ki} = \gamma_k s_n \) comprises the photodetector responsivity \( \gamma_k \) [A/W] and LED conversion factor \( s_n \) [W/A], \( D_{kn} \) is the distance between the \( k_{th} \) receiver and the \( i_{th} \) LED in the \( n_{th} \) LED luminary, \( \psi_{kn} \) is the angle of incidence at which the light is received relative to the normal vector of the receiver plane, \( \phi_{kn} \) is the angle of irradiance at which the light is emitted relative to the normal vector of the transmitter plane. \( T(\psi_{kn}) \) is the gain of the optical filter at the receiver. Furthermore, \( \mathbb{I}_A(\psi_{kn}) \) denotes the indicator function, and \( A = \{ \psi_{kn}, 0 \leq \psi_{kn} \leq \psi_e \} \), where \( \psi_e \) is the width of the field of view (FOV) at a receiver. The Lambertian radiant intensity is given by

\[
R(\phi_{kn}) = \frac{(m+1) \cos^m(\phi_{kn})}{2\pi},
\]

where \( m \) is the Lambertian order and specifies the transmit

Figure 1: Illustration of indoor coordinated VLC broadcast system.
beam divergence:
\[
m = -\frac{\log(2)}{\log(\cos(\phi_2/2))},
\]
where \(\phi_2\) is the transmitter semiangle. The receiver collection area \(A_k\) of the \(k\)th user can be expressed as
\[
A_k = \frac{\kappa^2}{\sin^2(\psi_c)} A_{PD}^k,
\]
where \(A_{PD}^k\) is the area of photodetector and \(\kappa\) is the concentrator refractive index.

The receiver-side noise term \(z_k\) (see (12) below) can be written as
\[
z_k = i_k + n_k,
\]
where \(i_k\) is the interference from neighbouring CoMP-attocells with average received electrical power \(E(i_k^2) = \sigma_i^2\), and the VLC noise component \(n_k\) comprises shot and thermal noise. We assume that \(n_k\) can be modelled as zero-mean Gaussian variable with variance [20]
\[
\sigma^2_{n_k} = 2eB(I_{tp}^k + I_{bg} I_2) + \sigma^2_{th},
\]
where \(e\) is the elemental charge, \(B\) is system bandwidth, \(I_{bg}\) is background current, \(I_2\) is the noise bandwidth factor (second Personick integral [21]), and \(\sigma^2_{th}\) is the thermal-noise variance. \(I_{tp}^k\) is the average current due to the received signal at the \(k\)th receiver. Denoting \(N_t\) the number of LED luminaries in one CoMP-attocell and \(I_{DC}^n\) the DC current of the \(n\)th LED luminary, \(I_{tp}^k\) is given by
\[
I_{tp}^k = \sum_{n=1}^{N_t} I_{DC}^n h_{kn}.
\]
We observe that \(I_{tp}^k\) is dependent on the DC current and thus illumination level and on user location, via \(h_{kn}\). This renders the optimization of broadcast transmission intractable. Therefore, we will use a fixed upper bound for \(I_{tp}^k\) in the following optimization. The accurate noise power is however applied for all numerical results.

Finally, we denote the total interference and noise power as
\[
\sigma_k^2 = E(z_k^2) = \sigma_i^2 + \sigma^2_{n_k}.
\]

\[B. \] Broadcast Transmission

In a VLC CoMP-attocell, \(N_t\) LED luminaries cooperate to broadcast information to \(N_t\) single-photodiode users. On-off keying (OOK) is applied in this work due to its popularity in optical communications and ease of implementation [22].

This is accomplished by modulating a zero-mean data signal onto the DC bias currents \(I_{DC} = [I_{DC}^1, \ldots, I_{DC}^{N_t}]^T\), which determine the brightness levels of the \(N_t\) LED luminaries. In the following, we describe the pre-processing of this data signal.

Let us denote \(d_k \in \{\pm 1\}\) the binary data symbol intended for the \(k\)th user, and \(d = [d_1, \ldots, d_{N_t}]^T\) is the data vector for all users with covariance matrix
\[
C_d = I.
\]

The broadcast signal for VLC MU-MISO is generated through linear precoding of the data vector with the matrix \(W\), i.e.,
\[
s = [s_1, \ldots, s_{N_t}]^T = W d.
\]

Finally, the transmitted signal is given as
\[
x = W d + I_{DC}.
\]

We note that the conversion to a current signal and the scaling of the binary data vector \(d\) is accomplished through matrix \(W\). Hence, choosing \(d_k \in \{\pm 1\}\) is without loss of generality. Furthermore, in VLC transmission, the elements of \(x\) must be non-negative, which imposes constraints on \(W\) as we will discuss further below.

Collecting the channel gains \(h_{kn}\) from (1) for all \(N_r \times N_t\) links into the channel matrix \(H = [h_1, \ldots, h_{N_t}]^T = \{h_{kn}\}_{N_t \times N_t}\), the received signal at the \(k\)th user can be written as
\[
\hat{y}_k = h_k^T x + z_k = h_k^T w_k d_k + h_k^T \sum_{i\neq k} w_i d_i + z_k + h_k^T I_{DC},
\]
where \(w_k\) represents the \(k\)th column of \(W\). The first term \(h_k^T w_k d_k\) is the desired signal, while the second term \(h_k^T \sum_{i\neq k} w_i d_i\) represents the intra-CoMP-attocell interference. The third term \(z_k\) is the sum of inter-CoMP-attocell interference and noise as introduced in (5). The fourth term \(h_k^T I_{DC}\) is the DC photocurrent for illumination that carries no data. It is removed via AC coupling at the receiver side, providing the information-carrying signal at the \(k\)th receiver as
\[
y_k = \hat{y}_k - h_k^T I_{DC} = h_k^T w_k d_k + h_k^T \sum_{i\neq k} w_i d_i + z_k.
\]

\[C. \] Constraints on Precoding from VLC

Consider the precoding operation in (10), the data signal \(s_n\) at the \(n\)th luminary satisfies
\[
-\|w_n\|_1 \leq s_n \leq \|w_n\|_1,
\]
where \(w_n\) is the \(n\)th row vector of the precoding matrix \(W\). After adding the DC bias, \(I_{DC}^n\), to adjust the brightness of each LED luminary, the electrical transmit signal (drive current) at the \(n\)th LED luminary is (see (11))
\[
x_n = s_n + I_{DC}^n.
\]
For simplicity, in the following we assume the same brightness level for every LED luminary, i.e.,
\[
I_{DC}^n = I_{DC}, \quad \forall n.
\]

Due to optical intensity modulation, \(x_n \geq 0\) and thus \(s_n \geq -I_{DC}\) from (15). However, similar to the nonlinearity of RF transmitters, LEDs also have a limited linear range [23]. While pre-distortion can be used to (approximately) linearize transmission, signal clipping needs to be avoided.

\[1\]Higher-order pulse-amplitude modulation schemes could also be employed in the case of high SINRs at the receivers. The precoder design would follow a similar approach as shown here for OOK.
Furthermore, if the LED is over-driven, not only will LED life-expectancy be reduced, but the self-heating effect will lead to a drop in the electrical-to-optical conversion efficiency. Considering these characteristics of LEDs, the transmit signal of each LED luminary should satisfy

\[ I_L \leq s_n + I_{DC} \leq I_U, \]

where \( I_U > I_L > 0 \) represent the upper and the lower bound of the LED drive current in the linear region. Substituting this into (14), we get

\[ I_{DC} - \| w_n \|_1 \geq I_L \]
\[ I_{DC} + \| w_n \|_1 \leq I_U \]

and the constraint

\[ \| w_n \|_1 \leq \min (I_{DC} - I_L, I_U - I_{DC}) \]

for the \( n_{th} \) row vector of the precoder matrix \( W \). Note that, via \( I_{DC} \), this constraint ties possible choices of VLC precoding matrices \( W \) to the user-selected illumination level of the LEDs.

D. Design Objectives

Given the broadcast transmission model (13) and constraint (19), we optimize the precoding represented by \( W \) in two ways. First, we consider the perhaps more obvious design task of maximizing the performance of MU-MISO VLC under illumination constraints, i.e., a given value of \( I_{DC} \). As an appropriate performance measure for MU-MISO VLC we adopt the sum mean-square error (sum-MSE). Secondly, we consider a VLC performance target represented by a given set of MSE thresholds for all users, and find the minimal illumination level required to maintain performance. This design provides a guaranteed VLC performance under different dimming levels. The two design objectives are pursued in Section III, assuming that perfect CSI, i.e., channel gains \( h_{kn} \) (1), are available at the VLC transmitters. In Section IV, we extend our derivations to the practically relevant case of imperfect channel knowledge at the transmitter.

III. Precoder Design with Perfect CSI

As mentioned above, the performance metric for precoder design adopted in this work is the sum MSE, which has widely been considered for precoding optimization in RF wireless MIMO/MISO systems, e.g., [24]. In particular, we consider the modified MSE [25] between the received signal \( y_k \) at the \( k_{th} \) user and original data \( d_k \) given by

\[ \text{MSE}_k = \mathbb{E}_{d_k,z_k} \{ \| c(y_k - d_k) \|_2^2 \} \]
\[ = \mathbb{E}_{d,z} \{ \| c(h_k^T W d + z_k) - e_k^T d \|_2^2 \}, \]

where \( c \) is a scaling term, which does not need to be applied at the receiver but offers a required degree of freedom in the receiver filter optimization, and \( e_k \) denotes the \( k_{th} \) standard basis vector for the \( N_r \)-dimensional space,

\[ e_k = [0_{1 \times (k-1)} \ 1 \ 0_{1 \times (N_r-k)}]^T. \]

A. Sum-MSE Minimization Problem

We first consider the sum-MSE minimization under illumination constraints. In this case, the precoder optimization problem can be formulated as

\[ \text{P1} : (W^*, c^*) = \arg \min_{W, c} \sum_{k=1}^{N_r} \text{MSE}_k \]
\[ \text{C1} : \| w_n \|_1 \leq \min (I_{DC} - I_L, I_U - I_{DC}), \forall n \]

Using (20), the objective function in P1 can be written as

\[ f(W, c) = \sum_{k=1}^{N_r} \text{MSE}_k = \mathbb{E}_{d,z} \{ \| c y - d \|_2^2 \}. \]

The optimization problem P1 is not jointly convex in precoder \( W \) and scaling factor \( c \). We therefore use an alternating optimization approach to, possibly suboptimally, solve this problem. Specifically, we iteratively optimize \( W \) and \( c \) while fixing the other variable.

1) Fixing Receiver Gain \( c \): We assume a fixed receiver gain \( c \) and then optimize the precoder \( W \). In this case, it is convenient to define

\[ \sigma^2_{\text{sum}} = \sum_{k=1}^{N_r} \sigma_k^2 \]

and to write the sum-MSE as

\[ \mathbb{E}_{d,z} \{ \| c y - d \|_2^2 \} = \mathbb{E}_{d,n} \{ \| c(HWd + z) - d \|_2^2 \} \]
\[ = \| c(I - I^T) \text{vec}(W^T) - \text{vec}(I) \|_2^2 + c^2 \sigma^2_{\text{sum}} \]

Then, defining \( b = \text{vec}(I) \), \( A = H \otimes I \), \( w = \text{vec}(W^T) \), and \( V \) as the \( N_r N_r \times N_r N_r \) block-diagonal matrix of the \( N_r \times N_r \) all-one matrix, problem P1, for a fixed gain \( c \), can be transformed into

\[ \text{P2} : (w^*, t^*) = \arg \min_{w, t} \| cA w - b \|_2^2 + c^2 \sigma^2_{\text{sum}} \]
\[ \text{C1} : -t \leq w \leq t \]
\[ \text{C2} : Vt \leq \min (I_{DC} - I_L, I_U - I_{DC}) 1_{N_r \times 1} \]

where \( t \) is a slack variable. The constraints in this optimization problem are equivalent to the \( L_1 \)-norm constraint (19) resulting from the limited dynamic range of the LED. This problem is a convex quadratic programming problem and can be efficiently solved using, e.g., YALMIP or CVX toolbox [26], [27].

2) Fixing Precoder \( W \): Now we assume the precoder matrix \( W \) as fixed and optimize for \( c \). The optimization problem P1 with fixed precoder \( W \) can be simplified into

\[ \text{P3} : c^* = \arg \min_c \| cA w - b \|_2^2 + c^2 \sigma^2_{\text{sum}} . \]

The optimal \( c^* \) can now be computed as

\[ c^* = \frac{\text{sym}(b^T A w)}{\| A w \|_2^2 + \sigma^2_{\text{sum}}}, \]

where

\[ \text{sym}(X) = \frac{X + X^T}{2} \]

represents the symmetric part of a matrix \( X \).
B. Minimal Illumination Level Problem

We now turn to the question of what is the minimal illumination level needed to maintain a certain VLC performance, termed here as the “minimal illumination level problem” in this paper. This is important for illumination systems with dimming, for which VLC should be supported. Illumination is proportional to $I_{DC}$, which via (19) affects VLC precoding. Measuring VLC performance in terms of MSE and denoting by $q_k$ the constraint for the MSE of the $k_{th}$ user, the corresponding optimization problem can be formulated as

$$P4: (W^*, e^*, I_{DC}) = \arg \min_{W, e, I_{DC}} I_{DC}$$

subject to:

$$C1: \text{MSE}_k \leq q_k, \forall k$$

$$C2: \|w_n\|_1 \leq \min (I_{DC} - I_L, I_U - I_{DC}), \forall n$$

Writing

$$\text{MSE}_k = (c h_k^T W - e_k^T)(c h_k^T W - e_k^T)^T + c^2 \sigma_k^2$$

and defining

$$\zeta = 1/c,$$

$$v_k^T = (h_k^T W - \zeta e_k^T),$$

$$\phi_k = [v_k^T \sigma_k],$$

the constraint $\text{MSE}_k \leq q_k$ can be expressed as

$$\|\phi_k\|_2 \leq \sqrt{q_k} \zeta.$$ \hspace{1cm} (32)

According to the Schur complement lemma [28][29], inequality (32) is equivalent to

$$\Theta_k = \begin{bmatrix} \sqrt{q_k} \zeta & \phi_k \\ \phi_k^T & \sqrt{q_k} I \end{bmatrix} \succeq 0.$$ \hspace{1cm} (33)

Thus, $P4$ can be reformulated as

$$P5: (W^*, \zeta^*, I_{DC}) = \arg \min_{W, \zeta, I_{DC}} I_{DC}$$

subject to:

$$C1: -t_k \leq W^T e_k \leq t_k, \forall k$$

$$C2: \|v_k\|_1 \leq \min (I_{DC} - I_L, I_U - I_{DC}), \forall k$$

$$C3: \Theta_k \succeq 0, \forall k$$

where vector $t_k$ is a slack variable. The problem is a convex semidefinite programming problem (SDP) and can be solved efficiently numerically, e.g., [26], [27].

IV. Precoder Design with Channel Uncertainty

The quality of CSI at the transmitter is critical to the precoder design. While the VLC channel is much more benign than its RF counterpart, the assumption of perfect CSI is not necessarily practical for MU-MISO VLC. VLC systems use visible light as the downlink medium, while the uplink medium can be RF, infrared light (IR) or visible light [30]. In the case of VLC uplink, the uplink-downlink reciprocity will allow CSI to be estimated at the transmitter. The more practically relevant scenario for VLC using indoor illumination devices considered here is that an RF uplink is used. In this case, CSI can only be estimated at the receiver and fed back to the transmitter afterwards. Imperfect CSI can then arise from noisy and quantized channel estimation and, perhaps more critically, the feedback of outdated estimates. The latter is the case when the VLC channel varies due to terminal motion and/or changes in the environment since the last channel update. As an example, Figure 2 illustrates a scenario where the receiver terminal has moved from position $p_1$, at which CSI is reported, to position $p_2$, at which precoded data using this CSI is received.

A. Uncertainty Models

Given the channel estimate $\hat{h}_k$, we can express the true channel gains for the $k_{th}$ user as

$$h_k = \hat{h}_k + \delta_k,$$ \hspace{1cm} (34)

where the error vector $\delta_k$ represents the CSI uncertainty. According to the source of estimation error, we consider two models for $\delta_k$.

1) Noisy CSI: For noisy CSI, we use the stochastic error model [28]

$$\delta_k \sim \mathcal{N}(0, \Sigma_k),$$ \hspace{1cm} (35)

i.e., $\delta_k$ is zero-mean Gaussian distributed with covariance matrix $\Sigma_k$.

2) Outdated CSI: Outdated CSI, due to e.g. a user walking with a terminal device (see Figure 2), is often modelled by a bounded uncertainty model, i.e.,

$$\|\delta_k\|_2 \leq \epsilon_k$$ \hspace{1cm} (36)

for some error bound $\epsilon_k$, which depends on the maximal changes that happened between CSI estimation and transmission using this estimation. As we show in the following, $\epsilon_k$ should be chosen as a function of the terminal location during channel estimation, i.e., $p_1$ in Figure 2. Location information could be obtained from channel estimation itself using various positioning techniques [31], [32].

Referring to Figure 2, we denote $L$ as the bound for the user movement between two CSI updates, i.e., $\|p_1 - p_2\|_2 \leq L$. Furthermore, considering a single transmitter, let $d_v$ and $d_h$ be the vertical and horizontal distance between transmitter and receiver, respectively, as indicated in Figure 2. Then, for terminal movement in horizontal direction, horizontal planes at the LED transmitter and photodiode receiver, and constant optical filter gain $T(\psi_{kn}) = T_k$, the error bound

$$\epsilon_k = \max\{\epsilon_+, \epsilon_-\}$$ \hspace{1cm} (37)
Figure 3: Error bounds obtained from simulation for (a): $L = 0.25$ m, (b): $L = 0.5$ m. Illumination and VLC setup for these results are described in Section V.

B. Sum-MSE Minimization Problem

We start with the sum-MSE minimization problem.

1) Robust Design with Outdated CSI: The robust broadcast precoder design for CSI uncertainty according to (36) is an extension of P1 in (22):

$$\text{P6}: (W^*, c^*) = \arg \min \max_{W,c} \max_{\|d_k\| \leq \epsilon_k} \sum_{k=1}^{N_t} \text{MSE}_k$$

$$\text{C1}: \|w_n\|_1 \leq \min (I_{DC} - I_L, I_U - I_{DC}), \forall n$$

where

$$\text{MSE}_k = \|c(\hat{h}_k^T + \delta_k^T)W - e_k^T\|^2_2 + c^2\sigma^2_k.$$ (44)

Using results from [28], P6 can be transformed into

$$\text{P7}: (W^*, c^*) = \arg \min \max_{W,c} \sum_{k=1}^{N_t} \text{MSE}_k$$

$$\text{C1}: -t_k \leq W^T e_k \leq t_k, \forall k$$

$$\text{C2}: \|W^T t_k \leq \min (I_{DC} - I_L, I_U - I_{DC}), \forall k$$

$$\text{C3}: \|w_n\|_1 \leq \min (I_{DC} - I_L, I_U - I_{DC}), \forall n$$

$$\text{C4}: \Phi \succeq 0$$

where

$$\Phi = \begin{bmatrix} g^2 & \lambda^T & c\sigma_{\text{sum}} \\ \lambda & gI & 0 \\ c\sigma_{\text{sum}} & 0 & g \end{bmatrix}$$

$$\Psi_k = \begin{bmatrix} \lambda_k - \mu_k & 0^T & c\hat{r}_k^T W - e_k^T \\ 0 & \mu_k I & \epsilon_k cW \\ (c\hat{r}_k^T W - e_k^T)^T & \epsilon_k (cW)^T & \lambda_k I \end{bmatrix}$$

Similar to the optimization problem P1, we can obtain a local optimum of this problem by alternatively optimizing over $W$ and $c$. Each problem is an SDP problem and can be efficiently solved numerically, e.g., [26], [27].

2) Robust Design with Noisy CSI: As noted above, the average sum-MSE is considered. Defining $\Delta = [\delta_1, \ldots, \delta_{N_r}]^T$, the optimization problem can be formulated as

$$\text{P8}: (W^*, c^*) = \arg \min_{W,c} \mathbb{E}_\Delta \left( \sum_{k=1}^{N_t} \text{MSE}_k \right)$$

$$\text{C1}: \|w_n\|_1 \leq \min (I_{DC} - I_L, I_U - I_{DC}), \forall n$$

Following the steps in (23) and (25) and assuming $\Sigma_k = \sigma^2_k I$, we can write the objective of P8 as

$$\mathbb{E}_\Delta (f(W, c)) = (\|cA\hat{w} - b\|^2_2 + N_t\sigma^2_k c^2 \|w\|^2_2) + c^2\sigma^2_{\text{sum}},$$ (48)

where $A = \hat{H} \otimes I$, and $\hat{H}$ is the estimated channel matrix. While P8 is not a convex optimization problem, again the application of alternating optimization for $W$ and $c$ turns out to be a suitable approach. When fixing the receiver gain $c$, we can optimize for $W$ via

$$\text{P9}: (w^*, t^*) = \arg \min_{w,t} (\|cA\hat{w} - b\|^2_2 + N_t\sigma^2_k c^2 \|w\|^2_2) + c^2\sigma^2_{\text{sum}},$$ (49)

$$\text{C1}: -t \leq w \leq t$$

$$\text{C2}: Vt \leq \min (I_{DC} - I_L, I_U - I_{DC}) 1_{N_x \times 1}$$

This problem is a convex quadratic programming problem, which is solved numerically. Fixing the precoder $W$ leads to the closed-form solution

$$c^* = \arg \min_c \left( \|cA\hat{w} - b\|^2_2 + N_t\sigma^2_k c^2 \|w\|^2_2 \right) + c^2\sigma^2_{\text{sum}}$$

$$= \frac{\text{sym}(b^T \hat{A} w)}{\|A\hat{w}\|^2_2 + N_t\sigma^2_k \|w\|^2_2 + \sigma^2_{\text{sum}}}.$$ (50)
C. Minimal Illumination Level Problem

We finally turn to the robust design for minimizing the required illumination level for a given VLC performance.

1) Robust Design with Outdated CSI: To add robustness to the precoder design for minimal required brightness when CSI is outdated, the worst-case MSE needs to satisfy the required performance \( q_k \):

\[
\max_{\| \delta_k \|_2 \leq \delta} \text{MSE}_k \leq q_k, \forall k \quad (51)
\]

Making use of the Schur complement lemma [28][29] and [33, Lemma 2], (51) is equivalent to \( \exists \lambda_k \geq 0, \)

\[
\Psi_k = \begin{bmatrix}
\sqrt{q_k} \zeta - \lambda_k & \hat{v}_k^T & \sigma_k & 0 \\
\hat{v}_k & \sqrt{q_k} I & 0 & -\epsilon_k W^T \\
\sigma_k & 0 & 0 & 0 \\
0 & -\epsilon_k W & 0 & \lambda_k I
\end{bmatrix} \succeq 0,
\]

where

\[
\hat{v}_k^T = (\hat{h}_k^T W - \zeta e_k^T).
\]

Hence, we obtain the optimization problem

\[
P10 : (W^*, \zeta^*, I_{DC}^*) = \arg\min_{W,A,\zeta,I_{DC}} I_{DC}
\]

\[
C1 : -t_k \leq W^T e_k \leq t_k, \forall k \\
C2 : 1^T t_k \leq \min (I_{DC} - I_L, I_U - I_{DC}), \forall k \\
C3 : \Psi_k \succeq 0, \forall k \\
C4 : \lambda_k \geq 0, \forall k
\]

This problem is an SDP and the global optimum can be obtained on condition that it is feasible.

2) Robust Design with Noisy CSI: In the case of noisy CSI, we need to replace C1 in P4 (29) by

\[
E_{\delta_k}(\text{MSE}_k) = c^2 \hat{v}_k^T \hat{v}_k + c^2 \sigma_k^2 \| W \|_F^2 + c^2 \sigma_k^2 .
\]

Introducing auxiliary variable \( r \) and \( r_k = [\hat{v}_k^T \ r \ \sigma_k] \),

\[
E_{\delta_k}(\text{MSE}_k) \leq q_k \text{ becomes equivalent to}
\]

\[
\| r_k \|_2 \leq \sqrt{q_k} \zeta, \\
\| W \|_F \leq \frac{r_k}{\sigma_k}
\]

Therefore, we can formulate the precoder design problem as

\[
P11 : (W^*, \zeta^*, I_{DC}^*) = \arg\min_{W,\{t_k\},\{r_k\},\zeta,I_{DC}} I_{DC}
\]

\[
C1 : -t_k \leq W^T e_k \leq t_k, \forall k \\
C2 : 1^T t_k \leq \min (I_{DC} - I_L, I_U - I_{DC}), \forall k \\
C3 : \| W \|_F \leq \frac{r_k}{\sigma_k} \\
C4 : \Psi_k \succeq 0, \forall k
\]

where

\[
\Psi_k = \begin{bmatrix}
\sqrt{q_k} \zeta & \tau_k & \sqrt{q_k} \zeta I
\end{bmatrix}.
\]

This problem is again an SDP.

V. NUMERICAL RESULTS AND DISCUSSIONS

In this section, we present and discuss the simulation results for the proposed MU-MISO VLC system assuming different coordination levels, user positions, interference levels and channel uncertainty scenarios in an indoor environment. We consider an example setup of a room with \( N_t = 4 \) coordinated and VLC-enabled LED luminaries at the ceiling. Room dimensions and luminary locations are listed in Table I. The table also summarizes the luminary and LED parameters, where the latter apply to LXW8-PW40 Luxeon Rebel high power LEDs [34]. The illuminance level when \( I_{DC} = 500 \) mA, i.e., \( I_{DC} = (I_L + I_U)/2 \), with this system setup is shown in Figure 4. According to [35], the illuminance level and uniformity (0.645 in this case) is sufficient for office work and study. The background current of \( I_{bg} = 100 \) µA accounts for ambient light from other sources such as sunlight or non-VLC enabled luminaries, and the thermal noise is considered negligible. We confirmed via measurements that these are valid assumptions.\(^2\)

In the following, we assume that the VLC system transmits to \( N_t = 4 \) users. For concreteness, we further assume that the four users are centro-symmetrically located on the plane at height \( z = 0.8 \) m, i.e., the user coordinates are \((\pm x, \pm y, 0.8)\) m for some \( x \) and \( y \). We would like to emphasize that the specific system parameters, in particular the values of \( N_t \) and \( N_r \), are chosen for the sake of illustration of precoded transmission only, and that our system design approach is applicable to any parameter pair \((N_t, N_r)\).

In the subsequent sections, we report performance results for different transmission scenarios and precoder designs. Due to symmetry, the performance for the \( N_t = 4 \) users are

\[\text{Table I: Simulation parameters.}\]

<table>
<thead>
<tr>
<th>Room Setup</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fixture coordinate 1</td>
</tr>
<tr>
<td>Fixture coordinate 2</td>
</tr>
<tr>
<td>Fixture coordinate 3</td>
</tr>
<tr>
<td>Fixture coordinate 4</td>
</tr>
<tr>
<td>Room Length ( L \times W \times H )</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Transmitter Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>( I_L )</td>
</tr>
<tr>
<td>( I_U )</td>
</tr>
<tr>
<td>Semi-angle at half power ( \phi_2 )</td>
</tr>
<tr>
<td>Dimensions of LED ( L \times W \times H )</td>
</tr>
<tr>
<td>LED interval</td>
</tr>
<tr>
<td>Number of LEDs per luminary ( K )</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Receiver Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>PD area</td>
</tr>
<tr>
<td>Refractive index of optical concentrator ( \kappa )</td>
</tr>
<tr>
<td>Gain of optical filter</td>
</tr>
<tr>
<td>Receiver FOV</td>
</tr>
<tr>
<td>System bandwidth ( B )</td>
</tr>
<tr>
<td>Noise bandwidth factor ( I_s )</td>
</tr>
<tr>
<td>Background current ( I_{bg} )</td>
</tr>
<tr>
<td>LED conversion factor ( s )</td>
</tr>
<tr>
<td>PD responsivity ( \gamma )</td>
</tr>
</tbody>
</table>

\[\text{\(^2\)We also ran simulations assuming larger } I_{bg} \text{ values of 620 µA [36] and even 5 mA [20], where especially the latter can be considered as an extreme worst-case noise scenario. We found however that the main trends of our results as discussed in the following are not affected by the value of the background current.}\]
identical, and thus we can drop the user index for the results. If not stated otherwise, perfect CSI for the precoder design is assumed. For solving the convex optimization problems in this paper, we use the YALMIP toolbox [26] in conjunction with the MOSEK solver [37] to obtain the result numerically. For solving the sum-MSE minimization problems via alternating optimization, the zero-forcing solution is used for initialization and the maximum number of iterations is set to 20.

A. User Position with Full Coordination Setup

We first investigate the achievable performance for a VLC broadcast system where LED luminaries are fully connected by a PLC backbone network and coordinated by a PLC controller. The users are arranged in three different setups as shown in the first three arrangements in Fig. 5, where $x = y = 0.5$ in Setup I, $x = y = 1.25$ in Setup II and $x = y = 2$ in Setup III, respectively. The channel matrices for these three setups are obtained as


$$H_{II} = 10^{-5} \begin{bmatrix} 9.340 & 1.788 & 0.731 & 1.788 \\ 1.788 & 9.340 & 1.788 & 0.731 \\ 0.731 & 1.788 & 9.340 & 1.788 \\ 1.788 & 0.731 & 1.788 & 9.340 \end{bmatrix}$$

$$H_{III} = 10^{-5} \begin{bmatrix} 6.164 & 0.863 & 0.000 & 0.863 \\ 0.863 & 6.164 & 0.863 & 0.000 \\ 0.000 & 0.863 & 6.164 & 0.863 \\ 0.863 & 0.000 & 0.863 & 6.164 \end{bmatrix}$$

Figure 6 shows the results of the sum-MSE minimization problem as a function of the DC bias $I_{DC}$, i.e., the illumination level, for the three user-configurations from Fig. 5. Here we use the resulting optimal precoder to calculate the corresponding SINR defined as

$$\text{SINR} = \frac{\|h_k^T w_k\|^2}{\|h_k^T \sum_{i \neq k} w_i\|^2 + \sigma_k^2}. \quad (57)$$

First, we observe that the system performance is symmetric with respect to $I_{DC} = (I_L + I_U)/2$. The SINR first increases as the DC bias $I_{DC}$ increases and then starts to decrease after $I_{DC}$ surpasses $(I_L + I_U)/2$. This is because the electrical SINRs at the receivers reach their maximal values when the precoded signal $s_n$ has the largest dynamic range. Due to this symmetry property, we will only plot the results for $I_{DC}$ ranging from $I_L$ to $(I_L + I_U)/2$ in the following figures. For varying positions of the four users, the setups in increasing order of SINR value are Setup I, Setup III and Setup II. An intuitive explanation is that since the users in Setup I are closer to each other than in Setup III, the channels are more similar and thus more difficult to separate through precoding. Meanwhile, the distances between the LED luminaries and users in Setup III are larger than those in Setup II, which leads to smaller channel gains in Setup III than in Setup II.

B. Different Transmitter Coordination Level

We now highlight the benefit of coordination. Therefore, and only in this section, we compare systems with different values for $N_I$ and $N_U$. More specifically, we consider three different coordination levels:
Figure 7: Different transmitter coordination levels in an MU-MISO VLC system.

1) **Fully coordinated (FC) system**: Transmissions for all four LED luminaries are coordinated, i.e., $N_t = N_r = 4$.

2) **Partially coordinated (PC) system**: Transmissions for LED luminaries in the first and the fourth quadrant and for LED luminaries in the second and the third quadrant are coordinated. Thus there exist two VLC CoMP-attocells in one room and for each of these systems $N_t = N_r = 2$ applies.

3) **Uncoordinated (UC) system**: Transmissions at the four LED luminaries are not coordinated, which corresponds to four VLC CoMP-attocells in one room. Each of these systems has parameters $N_t = N_r = 1$.

The three coordination levels are illustrated in Fig. 7.

We consider two scenarios for user locations: Setup IV with $x = 2$, $y = 1.25$ and Setup V with $x = 0.5$, $y = 1.25$ as shown in Fig. 5. Figure 8 shows the SINR for precoder design minimizing the sum-MSE as a function of $I_{DC}$ for different coordination levels and user position scenarios. We observe that, since users are located closer to each other and/or the neighbouring CoMP-attocell boundary in Setup V than for Setup IV, the achievable SINR is generally higher for the latter. We can also see the significant SINR increase due to coordination. In particular, the FC setup is clearly outperforming the PC and UC systems, whose SINR saturates quickly due to inter-cell interference. For Setup V, there is no performance difference for UC and PC systems, which is due to the remaining large inter-CoMP-attocell interference in spite of the partial coordination. In the PC system, each VLC transmitter tends to mostly communicate to its closest receiver, which makes the PC system equivalent to a UC system.

The benefit of (full) coordination is further demonstrated by the plots in Figure 9, which show the SINR for one quadrant of the room and $I_{DC} = (I_L + I_U)/2$. Sum-MSE minimization problem with perfect CSI.

C. __Sum-MSE Minimization with Channel Uncertainty__

We now abandon the assumption of perfect CSI and consider channel uncertainty according to the models from Section IV-A. For the case of outdated CSI, we consider an assumed user location based on which we obtain a channel estimate $\hat{h}_k$. Then, given a distance bound $L$, we obtain a CSI bound $\epsilon_k$ from numerical evaluation as shown in Section IV-A (see Fig. 3). Given $\hat{h}_k$ and $\epsilon_k$, the precoder $W$ is obtained via P7 (45). Then, a set of actual channel gains $\mathbf{h}$ and associated SINRs (57) are generated by placing users uniformly at random into the uncertainty region. For the noisy CSI case, we use $\Sigma_k = \sigma_k^2 I$ and specify the error variance $\sigma_k^2$.

Figures 10 and 11 show the SINR performance for the FC system with robust precoder design according to the sum-MSE criterion. The results are shown as a function of the channel uncertainty and parametrized with DC bias $I_{DC}$. Setup II from Figure 5 with $x = 1.25$ and $y = 1.25$ is used to calculate the channel estimate $\hat{h}_k$ and 5000 possible channel realizations $\mathbf{h}_k$ either according to the uncertainty bound $\epsilon_k$ or the normalized
D. Minimal Illumination Level Problem

We again consider the Setup II from Figure 5 with $x = 1.25$ and $y = 1.25$, and FC. Figure 12 shows the minimum illumination level, i.e., DC bias $I_{DC}$, that is required to meet the VLC MSE levels $q_k$ of each user terminal. The different curves are for perfect CSI ($L = 0$) and outdated CSI ($L > 0$), and they quantify to what extent VLC is possible when lights are dimmed. The perfect CSI case shows the best possible trade-off between illumination level and achievable performance. When CSI uncertainty comes into play, it increases the required illumination level eventually limits the achievable performance. That is, the larger the uncertainty region (quantified by $L$), the earlier the problem becomes infeasible, i.e., MSE constraints cannot be met regardless of illumination level.

E. Comparison between Robust and Non-Robust Design

Finally, we illustrate the benefits of the robust design in the case of CSI uncertainty. To this end, Figure 13 compares the SINR performances of the robust and non-robust precoder designs when CSI is outdated. Similar to Figure 9, SINR performance for one quadrant of the room is plotted as a function of the assumed user location, according to which $h_k$ is obtained. The actual user location is sampled in a circle with radius $L$, from which the channel gain $h_k$ follows. Figure 13 shows, for each assumed location, the minimum SINR over the uncertainty region. The DC current $I_{DC}$ is fixed as $I_{DC} = (I_L + I_U)/2$.

We observe that especially for locations close to the boundaries of two cells the robust design significantly outperforms the non-robust approach. This is due to the possibly large mismatch between assumed and actual channel gains, which also affects the expected amount of interference, and which is not taken into account in the non-robust design approach. For example, for the case of $L=0.25$, the average SINR value on the boundaries of two cells is improved from $-25.99$ dB to $-0.69$ dB via the robust design. On the other hand, closer inspection of the results shows that for locations further from the boundaries between cells, the precoder from the non-robust design achieves a somewhat better SINR than the robust precoder. For example, at the location $(x, y) = (0.375, 1.000)$,
the worst-case SINR for the robust design is 4.4 dB, while it is 6.2 dB for the non-robust design. The reason for this is the conservativeness of the robust design, which considers the worst case for all hypothetical gains from the bounded region \( \mathcal{R}_k = \{ (h_k) \mid \| h_k \|_2 \leq c_k \} \), even though only a subset of these channel gains do actually occur inside the location uncertainty region. Nevertheless, the results in Figure 13 demonstrate the advantage of the robust optimization for VLC broadcasting in the case of imperfect CSI, in that the SINR is more consistently high over the entire attocell area and when different users are close to each other.

VI. CONCLUSION

In this paper, we have studied transmission to multiple user terminals using VLC attocells. Considering the inter-cell interference as a result of the broadcast nature of VLC, we have proposed the coordination of transmission in different attocells. These coordinated VLC attocells form CoMP-attocells, similar to CoMP-cells in RF cellular networks. We have derived new linear precoding schemes that reduce intra-CoMP-attocell interference with the objective of optimizing system performance given an illumination level and retaining a required performance at minimal illumination level, respectively. Our numerical results for a typical VLC scenario have clearly demonstrated the improvements of receiver-side SINR due to the proposed coordination. As a second important contribution, we have extended the precoding methods to include channel uncertainty, which would occur, for example, in the case of moving terminals. Simulation results have shown that these robust precoding schemes mitigate performance drops that stale channel information causes.

ACKNOWLEDGMENT

The authors would like to thank Mr. Warren Pawlikowski for his VLC noise measurements that helped choosing realistic parameters in this work.

REFERENCES


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